

IDENTIDADES AUXILIARES

Demostrar: $\tan x + \cot x = \sec x \cdot \csc x$

$$\tan x + \cot x = \frac{\sin x}{\cos x} + \frac{\cos x}{\sin x}$$

$$\tan x + \cot x = \frac{\sin x \sin x + \cos x \cos x}{\cos x \sin x}$$

$$\tan x + \cot x = \frac{1}{\cos x \sin x}$$

$$\tan x + \cot x = \frac{1}{\cos x} \cdot \frac{1}{\sin x}$$

$$\tan x + \cot x = \sec x \cdot \csc x \quad \text{lqgd}$$

Demostrar: $\sec^2 x + \csc^2 x = \sec^2 x \cdot \csc^2 x$

$$\sec^2 x + \csc^2 x = \frac{1}{\cos x \cos x} + \frac{1}{\sin x \sin x}$$

$$\sec^2 x + \csc^2 x = \frac{\sin x \sin x + \cos x \cos x}{\cos x \cos x \sin x \sin x}$$

$$\sec^2 x + \csc^2 x = \frac{1}{\cos x \cos x \sin x \sin x}$$

$$\sec^2 x + \csc^2 x = \frac{1}{\cos x \cos x} \cdot \frac{1}{\sin x \sin x}$$

$$\sec^2 x + \csc^2 x = \sec^2 x \cdot \csc^2 x \quad \text{lqgd}$$

$$\sin^2 x + \cos^2 x = 1$$

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Demostrar: $\sin^4 x + \cos^4 x = 1 - 2\sin^2 x \cdot \cos^2 x$

Sabemos: $\sin^2 x + \cos^2 x = 1$

$$(\sin^2 x + \cos^2 x)^2 = 1^2$$

$$\sin^4 x + \cos^4 x + 2\sin^2 x \cos^2 x = 1$$

$$\sin^4 x + \cos^4 x = 1 - 2\sin^2 x \cos^2 x \quad \text{lqgd}$$

$$(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$$

Demostrar: $\sin^6 x + \cos^6 x = 1 - 3\sin^2 x \cdot \cos^2 x$

Sabemos: $\sin^2 x + \cos^2 x = 1$

$$(\sin^2 x + \cos^2 x)^3 = 1^3$$

$$\sin^6 x + \cos^6 x + 3\sin^2 x \cos^2 x (\sin^2 x + \cos^2 x) = 1$$

$$\sin^6 x + \cos^6 x + 3\sin^2 x \cos^2 x (1) = 1$$

$$\sin^6 x + \cos^6 x + 3\sin^2 x \cos^2 x = 1$$

$$\sin^6 x + \cos^6 x = 1 - 3\sin^2 x \cos^2 x \dots \text{lqgd}$$

Demostrar: $(1 + \text{Sen}x + \text{Cos}x)^2 = 2(1 + \text{Sen}x)(1 + \text{Cos}x)$

$$(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + ac + bc)$$

$$(1 + \text{Sen}x + \text{Cos}x)^2 = 1^2 + \text{Sen}^2x + \text{Cos}^2x + 2(\text{Sen}x + \text{Cos}x + \text{Sen}x\text{Cos}x)$$

$$(1 + \text{Sen}x + \text{Cos}x)^2 = 1 + 1 + 2(\text{Sen}x + \text{Cos}x + \text{Sen}x\text{Cos}x)$$

$$(1 + \text{Sen}x + \text{Cos}x)^2 = 2 + 2(\text{Sen}x + \text{Cos}x + \text{Sen}x\text{Cos}x)$$

$$(1 + \text{Sen}x + \text{Cos}x)^2 = 2 + 2\text{Sen}x + 2\text{Cos}x + 2\text{Sen}x\text{Cos}x$$

$$(1 + \text{Sen}x + \text{Cos}x)^2 = 2(1 + \text{Sen}x) + 2\text{Cos}x(1 + \text{Sen}x)$$

$$(1 + \text{Sen}x + \text{Cos}x)^2 = (1 + \text{Sen}x)(2 + 2\text{Cos}x)$$

$$(1 + \text{Sen}x + \text{Cos}x)^2 = 2(1 + \text{Sen}x)(1 + \text{Cos}x) \quad \text{lqqd}$$

Demostrar: $(1 + \text{Sen}x - \text{Cos}x)^2 = 2(1 + \text{Sen}x)(1 - \text{Cos}x)$

$$(a + b - c)^2 = a^2 + b^2 + c^2 + 2(ab - ac - bc)$$

$$(1 + \text{Sen}x - \text{Cos}x)^2 = 1^2 + \text{Sen}^2x + \text{Cos}^2x + 2(\text{Sen}x - \text{Cos}x - \text{Sen}x\text{Cos}x)$$

$$(1 + \text{Sen}x - \text{Cos}x)^2 = 1 + 1 + 2(\text{Sen}x - \text{Cos}x - \text{Sen}x\text{Cos}x)$$

$$(1 + \text{Sen}x - \text{Cos}x)^2 = 2 + 2(\text{Sen}x - \text{Cos}x - \text{Sen}x\text{Cos}x)$$

$$(1 + \text{Sen}x - \text{Cos}x)^2 = 2 + 2\text{Sen}x - 2\text{Cos}x - 2\text{Sen}x\text{Cos}x$$

$$(1 + \text{Sen}x - \text{Cos}x)^2 = 2(1 + \text{Sen}x) - 2\text{Cos}x(1 + \text{Sen}x)$$

$$(1 + \text{Sen}x - \text{Cos}x)^2 = (1 + \text{Sen}x)(2 - 2\text{Cos}x)$$

$$(1 + \text{Sen}x - \text{Cos}x)^2 = 2(1 + \text{Sen}x)(1 - \text{Cos}x) \quad \text{lqqd}$$

Demostrar: $(1 - \text{Sen}x + \text{Cos}x)^2 = 2(1 - \text{Sen}x)(1 + \text{Cos}x)$

$$(a - b + c)^2 = a^2 + b^2 + c^2 - 2(ab + ac - bc)$$

$$(1 - \text{Sen}x + \text{Cos}x)^2 = 1^2 + \text{Sen}^2x + \text{Cos}^2x - 2(\text{Sen}x - \text{Cos}x + \text{Sen}x\text{Cos}x)$$

$$(1 - \text{Sen}x + \text{Cos}x)^2 = 1 + 1 - 2(\text{Sen}x - \text{Cos}x + \text{Sen}x\text{Cos}x)$$

$$(1 - \text{Sen}x + \text{Cos}x)^2 = 2 - 2(\text{Sen}x - \text{Cos}x + \text{Sen}x\text{Cos}x)$$

$$(1 - \text{Sen}x + \text{Cos}x)^2 = 2 - 2\text{Sen}x + 2\text{Cos}x - 2\text{Sen}x\text{Cos}x$$

$$(1 - \text{Sen}x + \text{Cos}x)^2 = 2(1 - \text{Sen}x) + 2\text{Cos}x(1 - \text{Sen}x)$$

$$(1 - \text{Sen}x + \text{Cos}x)^2 = (1 - \text{Sen}x)(2 + 2\text{Cos}x)$$

$$(1 - \text{Sen}x + \text{Cos}x)^2 = 2(1 - \text{Sen}x)(1 + \text{Cos}x) \quad \text{lqqd}$$

Demostrar: $(1 - \text{Sen}x - \text{Cos}x)^2 = 2(1 - \text{Sen}x)(1 - \text{Cos}x)$

$$(a - b - c)^2 = a^2 + b^2 + c^2 - 2(ab + ac - bc)$$

$$(1 - \text{Sen}x - \text{Cos}x)^2 = 1^2 + \text{Sen}^2x + \text{Cos}^2x - 2(\text{Sen}x + \text{Cos}x - \text{Sen}x\text{Cos}x)$$

$$(1 - \text{Sen}x - \text{Cos}x)^2 = 1 + 1 - 2(\text{Sen}x + \text{Cos}x - \text{Sen}x\text{Cos}x)$$

$$(1 - \text{Sen}x - \text{Cos}x)^2 = 2 - 2(\text{Sen}x + \text{Cos}x - \text{Sen}x\text{Cos}x)$$

$$(1 - \text{Sen}x - \text{Cos}x)^2 = 2 - 2\text{Sen}x - 2\text{Cos}x + 2\text{Sen}x\text{Cos}x$$

$$(1 - \text{Sen}x - \text{Cos}x)^2 = 2(1 - \text{Sen}x) - 2\text{Cos}x(1 - \text{Sen}x)$$

$$(1 - \text{Sen}x - \text{Cos}x)^2 = (1 - \text{Sen}x)(2 - 2\text{Cos}x)$$

$$(1 - \text{Sen}x - \text{Cos}x)^2 = 2(1 - \text{Sen}x)(1 - \text{Cos}x) \quad \text{lqqd}$$

Demostrar: $\frac{\cos x}{1 + \sin x} = \frac{1 - \sin x}{\cos x}$

$$\frac{\cos x (1 - \sin x)}{(1 + \sin x)(1 - \sin x)}$$

$$\frac{\cos x (1 - \sin x)}{1 - \sin^2 x}$$

$$\frac{\cos x (1 - \sin x)}{\cos^2 x}$$

$$\frac{1 - \sin x}{\cos x}$$

Demostrar: $\frac{\cos x}{1 - \sin x} = \frac{1 + \sin x}{\cos x}$

$$\frac{\cos x (1 + \sin x)}{(1 - \sin x)(1 + \sin x)}$$

$$\frac{\cos x (1 + \sin x)}{1 - \sin^2 x}$$

$$\frac{\cos x (1 + \sin x)}{\cos^2 x}$$

$$\frac{1 + \sin x}{\cos x}$$

Demostrar: $\frac{\sin x}{1 + \cos x} = \frac{1 - \cos x}{\sin x}$

$$\frac{\sin x (1 - \cos x)}{(1 + \cos x)(1 - \cos x)}$$

$$\frac{\sin x (1 - \cos x)}{1 - \cos^2 x}$$

$$\frac{\sin x (1 - \cos x)}{\sin^2 x}$$

$$\frac{1 - \cos x}{\sin x}$$

Demostrar: $\frac{\sin x}{1 - \cos x} = \frac{1 + \cos x}{\sin x}$

$$\frac{\sin x (1 + \cos x)}{(1 - \cos x)(1 + \cos x)}$$

$$\frac{\sin x (1 + \cos x)}{1 - \cos^2 x}$$

$$\frac{\sin x (1 + \cos x)}{\sin^2 x}$$

$$\frac{1 + \cos x}{\sin x}$$

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$$\text{Tan}x + \text{Ctg}x = \text{Sec}x \cdot \text{Csc}x$$

$$\text{Sec}^2x + \text{Csc}^2x = \text{Sec}^2x \cdot \text{Csc}^2x$$

$$\text{Sen}^4x + \text{Cos}^4x = 1 - 2\text{Sen}^2x \cdot \text{Cos}^2x$$

$$\text{Sen}^6x + \text{Cos}^6x = 1 - 3\text{Sen}^2x \cdot \text{Cos}^2x$$

$$(1 + \text{Sen}x + \text{Cos}x)^2 = 2(1 + \text{Sen}x)(1 + \text{Cos}x)$$

$$(1 + \text{Sen}x - \text{Cos}x)^2 = 2(1 + \text{Sen}x)(1 - \text{Cos}x)$$

$$(1 - \text{Sen}x + \text{Cos}x)^2 = 2(1 - \text{Sen}x)(1 + \text{Cos}x)$$

$$(1 - \text{Sen}x - \text{Cos}x)^2 = 2(1 - \text{Sen}x)(1 - \text{Cos}x)$$

Las identidades trigonométricas auxiliares adicionales

$$\frac{\text{Cos}x}{1 + \text{Sen}x} = \frac{1 - \text{Sen}x}{\text{Cos}x}$$

$$\frac{\text{Cos}x}{1 - \text{Sen}x} = \frac{1 + \text{Sen}x}{\text{Cos}x}$$

$$\frac{\text{Sen}x}{1 + \text{Cos}x} = \frac{1 - \text{Cos}x}{\text{Sen}x}$$

$$\frac{\text{Sen}x}{1 - \text{Cos}x} = \frac{1 + \text{Cos}x}{\text{Sen}x}$$